

# Operational modal analysis on a pump operating at varying speeds: an industrial history case

VU VIET-HUNG<sup>1</sup>, BADRI BECHIR<sup>1</sup>, THOMAS MARC<sup>1,a</sup> AND JEAN PIERRE<sup>2</sup>

<sup>1</sup> École de technologie supérieure, Montréal, Qc, H3C 1K3, Canada

<sup>2</sup> Ville de Montréal - Station d'épuration, Montréal, Qc, H1C 1V3, Canada

Received 3 April 2015, Accepted 18 June 2015

**Abstract** – Industrial hydraulic pumps are complex structures on which vibrations can be harmful for reliability, fatigue of components and productivity. The application of vibration analysis and diagnosis on a huge water treatment pump at the City of Montreal's facility is presented in this paper. By using a Short Time Auto-Regressive (STAR) method combined with a modal test, it is seen that the dynamic properties and behavior of the pump included both rotating and fixed structures can be evaluated from the experimental analysis on the vibration measurement signal during its normal working condition. Natural frequencies, damping ratios and rotating speed can be clearly identified and monitored. It is shown that the analysis and diagnosis from operational vibration measurement is a very effective technique for the assessment of the huge machines in real working condition.

**Key words:** Hydraulic pump / operational modal analysis / vibration diagnosis / short-time autoregressive

## Nomenclature

$\mathbf{A}_i$	Matrix of parameters relating the output $\mathbf{y}(t-i)$ to $\mathbf{y}(t)$
$d$	Vector dimension or number of sensors
$\mathbf{e}(t)$	Residual vector of all output channels
$p$	Model order
$t$	Time index
$T_s$	Sampling period
$\mathbf{y}(t-i)$	Output vector with time delay $i \times T_s$
$\mathbf{z}(t)$	Regressor for the output vector $\mathbf{y}(t)$
$\mathbf{\Lambda}$	Model parameters matrix

## 1 Introduction

Vibrations are detrimental for industrial machines and lack of reliability may come from these vibrations during the machine operation. In order to characterise the dynamic behaviour of the structures, modal analysis in non-operational conditions is a basic technique [1,2]. However, due to nonlinear behaviors of dynamic systems, modal analysis in the operational conditions of machines became a necessity to provide a better characterization, analysis and diagnosis in the real life broadband excitations, especially on huge dimension machines where the usual modal

testing suffers lack of applicability [3]. In this paper, this so called operational modal analysis is applied for the vibration analysis and diagnosis of a hydraulic pump in its normal operation [4]. A Short Time Auto-Regressive method (STAR) is used to identify and track the modal parameters of the machines during the operational vibrations. By analyzing the transient vibration signal from fixed and varying operational speeds, the analysis and diagnosis are able to identify the modal parameters and to discriminate the natural frequencies from the resonance frequencies.

## 2 The ebara hydraulic pump

A series of the EBARA pumps (Fig. 1) with three blades and operating at varying speeds is installed at the Montreal city's water treatment plant since the 1970's years. High amplitudes vibrations were witnessed on those pumps at operational speed near 350 RPM [5], and vibration analysis was called in order to identify those high amplitude vibration causes and by consequence to propose corrections.

## 3 Short-time autoregressive (STAR) model

Time series models such as the autoregressive (AR) or autoregressive moving average (ARMA) have been

<sup>a</sup> Corresponding author: marc.thomas@etsmtl.ca



Fig. 1. EBARA pump.

recently used for modal analysis on various applications. As the excitation is generally unknown in operational modal analysis, an AR model at higher order is equivalent to the ARMA model and can be used for the modeling with simple and rapid estimation algorithm. The STAR model has been developed for the operational modal analysis of non-stationary structures and rotating machines [4]. The core mathematic model in the STAR method is the vector-autoregressive (VAR) model where signals from multi channels measurements can be modelled as follows [4]:

$$\mathbf{y}(t) = \mathbf{\Lambda}\mathbf{z}(t) + \mathbf{e}(t) \quad (1)$$

where:

$\mathbf{\Lambda} = [-\mathbf{A}_1 \ -\mathbf{A}_2 \ \dots \ -\mathbf{A}_p]$  size  $d \times dp$  is the parameter matrix;

$\mathbf{A}_i$  (size  $d \times d$ ) is the matrix of parameters relating the output  $\mathbf{y}(t-i)$  to  $\mathbf{y}(t)$ ;

$\mathbf{z}(t) = \left[ \mathbf{y}(t-1)^T \ \mathbf{y}(t-2)^T \ \dots \ \mathbf{y}(t-p)^T \right]^T$  (size  $dp \times 1$ ) is the regressor for the output vector  $\mathbf{y}(t)$ ;

$\mathbf{y}(t-i)$  (size  $d \times 1$ ;  $i = 1 : p$ ) is the output vector with delay time  $i \times T_S$ ;

$\mathbf{e}(t)$  (size  $d \times 1$ ) is the residual vector of all output channels considered as the error of model.

The model is estimated by the least squares via the construction of the QR factorization [6] where detail about the signal to noise based model order selection method was also addressed. By applying the VAR model with a sliding window technique as shown in Figure 2, the STAR evolves in the time domain.

As the operation of the machines can deal with time varying effects such as loading, rotation speed or even damages, the operational vibrations usually come from non-stationary sources. To analyze the operational vibration signals, it is therefore beneficial to use the short time window which can be progressed successively in the time domain. In each window, the VAR model is considered stationary. The least squares solution is fast, stable and well-conditioned. Modal parameters are subsequently computed with sufficient accuracy. As the window moves forward, the method is able to track the non-stationary effect. Moreover, the updating of the VAR on model order directly from window to window allows the method for tracking quickly the changes on the system [7]. The advantages of the method are its ability to work fast, accurately online on multi channels measurements, the automation on modes and harmonics distinction [8], its ability to deal with non-stationary signals and with modal parameters uncertainty [9].

## 4 Analysis and diagnosis

### 4.1 Measurements at operational fixed speeds

The vibration measurement is first done on the pump at the constant speed of 360 RPM. Figure 3 shows two measurement positions on three directions RH: Radial Horizontal, RV: Radial Vertical, and RX: Radial Axial [10]. Figure 4 shows the time accelerations (in g) measured in three directions at two points A and B. At a glance, it is observed that the signal can be seen stationary and the vibrations exhibit not much difference in term of amplitudes between the two locations and in the three directions.

In order to compare the vibration levels with standards which are expressed in velocity, Figure 5 shows the velocity spectrum at low frequencies. The rotational frequency is 6 Hz. The main amplitudes are observed at the Blade Pass Frequency (BPF) (18 Hz:  $1.5$  to  $2.0 \text{ mm.s}^{-1}$ ) and at the fourth harmonic (24 Hz: amplitude  $3 \text{ mm.s}^{-1}$ ). A double frequency is observed at the 3rd harmonic, mostly at the point B. Since the pump is running in steady regime, the double frequency can be explained by a slight asymmetry on the pump structure.

By applying the VAR model presented above to the signal, we can on the other hand construct a stabilization diagram up to model order 50 for both points A and B. The stabilization diagram shows the natural frequencies identified at a range of model orders where the stable frequencies have more chance to be the natural frequencies of the machine. It is seen in Figure 6 the rotating frequency around 6 Hz which is only stable from model order 40. Two stable frequencies around 18 Hz and 24 Hz match

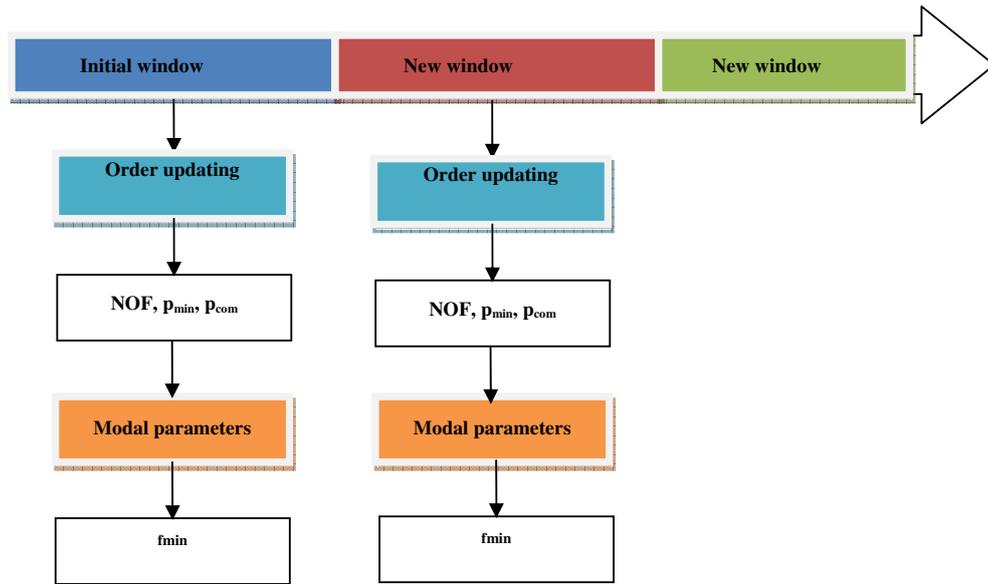


Fig. 2. STAR working scheme.



Fig. 3. Measurement locations.

well with the spectra given in Figure 5. However, the discrimination of the natural frequencies and the higher harmonics can be only clarified by the transient testing in the next section.

The RMS velocity ( $\text{mm}\cdot\text{s}^{-1}$ ), accelerations in RMS (mg) and Kurtosis are calculated in Table 1.

The RMS velocity may be compared to the ISO guide: Mechanical vibration – Evaluation of machine vibration by measurements on non-rotating parts – Part 7: Rotodynamic pumps for industrial applications, including measurements on rotating shafts (ISO 10816-7:2009) [11], as shown in Table 2.

By comparing the results, it is possible to say that the vibrations are on the limit of category C- Restricted long

term operation. The Kurtosis may be considered as high (greater than 3) [12]. With the data originally sampled at 51 200 Hz, Figure 7 shows the acceleration spectrum at high frequencies.

The vibration energy is spread mainly from 1500 Hz to 4500 Hz which may be caused by the presence of cavitation. However, the global effective level stays small (max is less than 400 mg), so the phenomena may be considered as acceptable.

#### 4.2 Transient testing

A transient test by varying the speed had been done on the same pump and the same accelerometers locations.

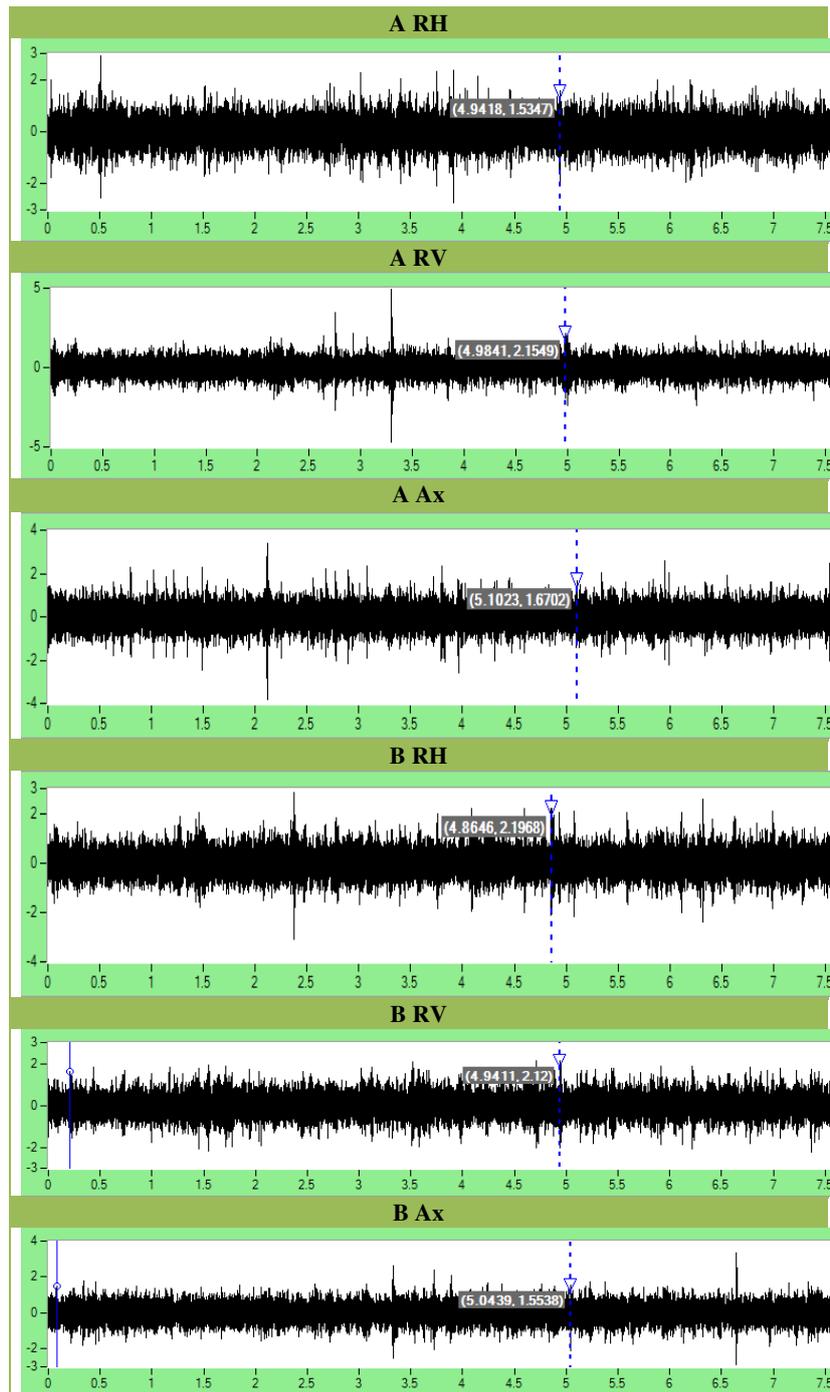


Fig. 4. Acceleration responses.

Table 1. Vibration indicators.

Machine	Point	Dir	RMS Velocity ( $\text{mm.s}^{-1}$ )	RMS (mg)	KU
GMP 10 - 1	A	RH	5.239	380	3.741
		RV	4.54	330	5.14
		Ax	4.27	305	3.386
	B	RH	4.699	375	3.919
		RV	3.996	351	3.678
		Ax	5.303	427	4.413

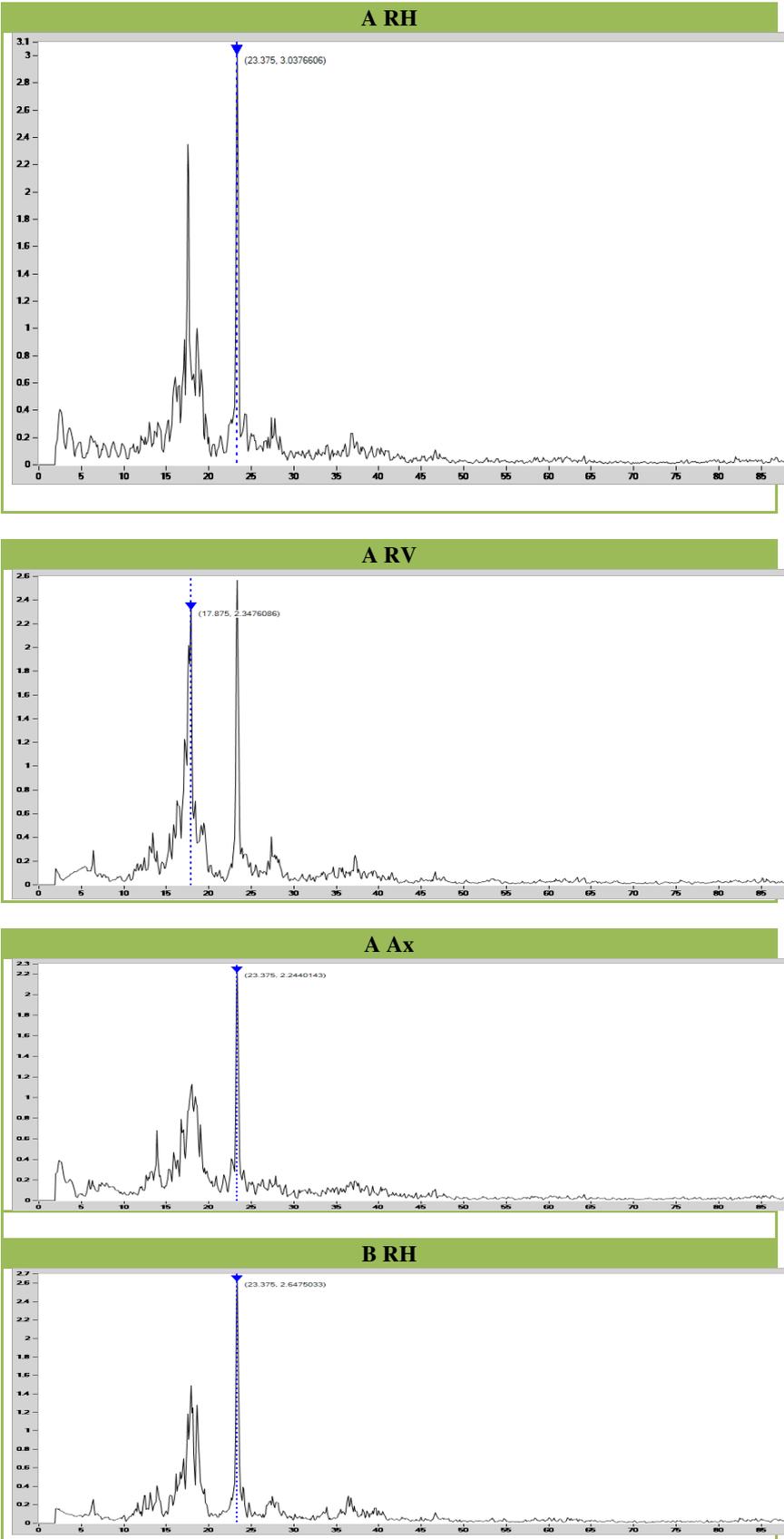


Fig. 5. Velocity spectrum.

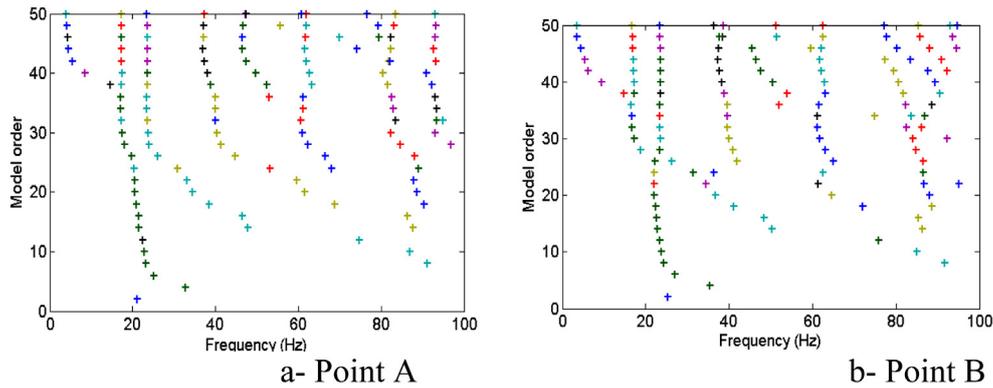


Fig. 6. Stabilization diagram

Table 2. ISO 10816-7:2009.

DIN ISO 10816-7	Category 1		Category 2		
Pump type	Rotodynamic pumps with high reliability, availability or security requirements.		Rotodynamic pumps for general or less critical applications.		r < 600 rpm
Power	< 200 kW	> 200 kW	< 200 kW	> 200 kW	0.5 rpm 1.0 rpm 2.0 rpm
Velocity $v_{eff}$	7,6	D	9,5	D	Displacement $s_{pp}$
	6,5		8,5		
10–1000 Hz $r > 600$ rpm	5,0	C	6,1	C	130
	4,0		5,1		80
2–1000 Hz $r < 600$ rpm	3,5	B	4,2	B	50
	2,5		3,2		$\mu m$
mm/s rms	A		mm/s rms	A	
A Newly commissioned machines		B Unrestricted long term operation		C Restricted long term operation	
				D Vibration causing damage	

The pump was set to run at the varying speeds from 385 RPM to 340 RPM during 45 s, and then stay at constant speed 340 RPM on the last 45 s. For structural modal analysis purpose, the data have been resampled at the frequency of 512 Hz (Fig. 8).

Applying the STAR method with a window length 2 s (1024 samples) and 50% overlapping, we can see the monitoring of the modal parameters during the non-stationary operation in Figure 9 (frequency monitoring) and Figure 10 (damping ratio monitoring). From the monitoring of the modal parameters obtained from only vibrational responses during the normal operation, it is possible to see that all the basic modes of the structure are present in the vibration spectra. All the modal parameters are stable during the operation when varying speed or at fixed speed, while the harmonic frequencies are varying (4th harmonic at 24 Hz). During the first half of the transient loading time, the operation speed varies from 385 RPM to 340 RPM whose the 4th harmonic is closed to the 2nd structural mode at 25 Hz.

A resonance occurs during the first half time and the STAR method therefore tracks the varying operational speed with the corresponding damping ratios close to

zero. During the 2nd half time, the STAR method identifies and tracks all the structural modes with constant natural frequencies around 18 Hz, 25 Hz, 38 Hz, 50 Hz, 62 Hz and stable damping ratios around 5%.

The monitoring results from the non-stationary vibration validate also the spectrum constructed from the fixed operational speed in the fixed speed testing section (Fig. 5). It is then well seen that the first structural mode is found around 18 Hz close to the BPF (third harmonic) and another resonance occurs near 25 Hz (close to 4th harmonic).

## 5 Preliminary solution proposals

It is seen from the diagnosis that a structural mode around 17–18 Hz is found close to the 3rd harmonic and another structural mode around 24 Hz is found close to the 4th harmonics. In order to avoid the resonance, a rough numerical model of the pump has been built in Ansys and several preliminary structural modifications are considered on the rotating and the fix parts respectively to modify the natural frequencies of those two structural

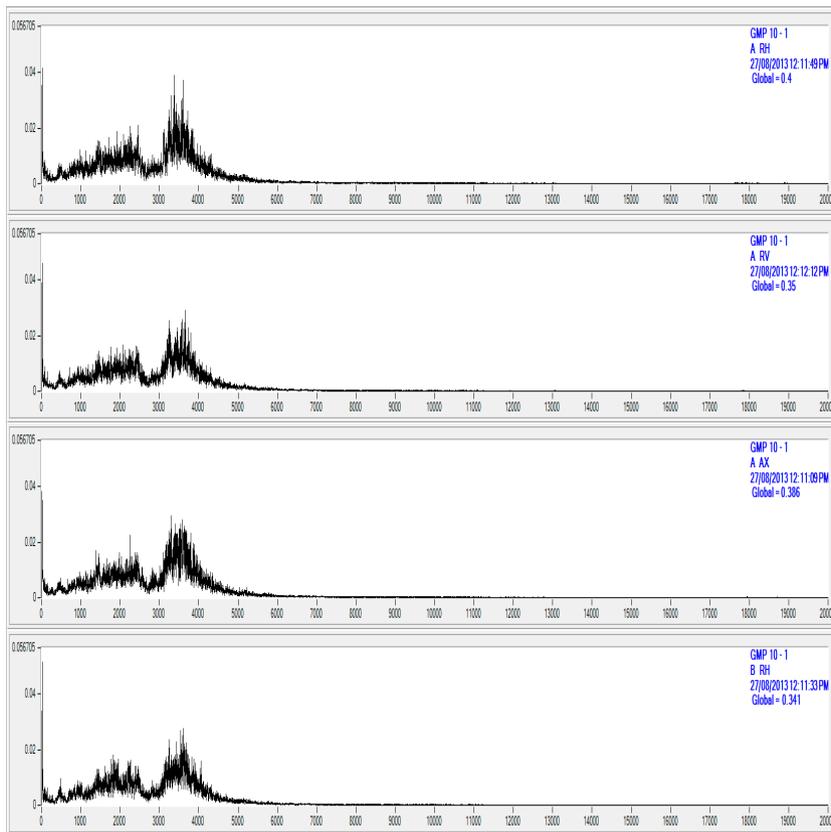


Fig. 7. Acceleration spectrums at high frequencies.

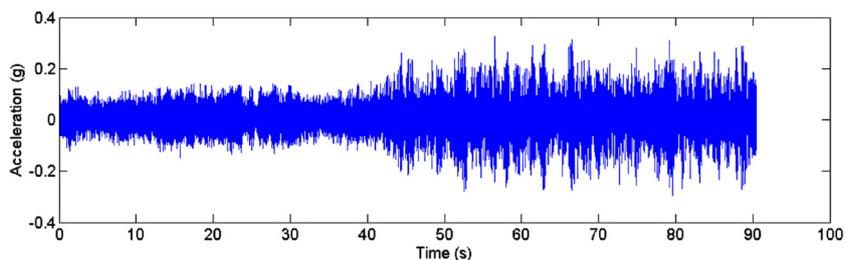


Fig. 8. Transient operational signal, point A.

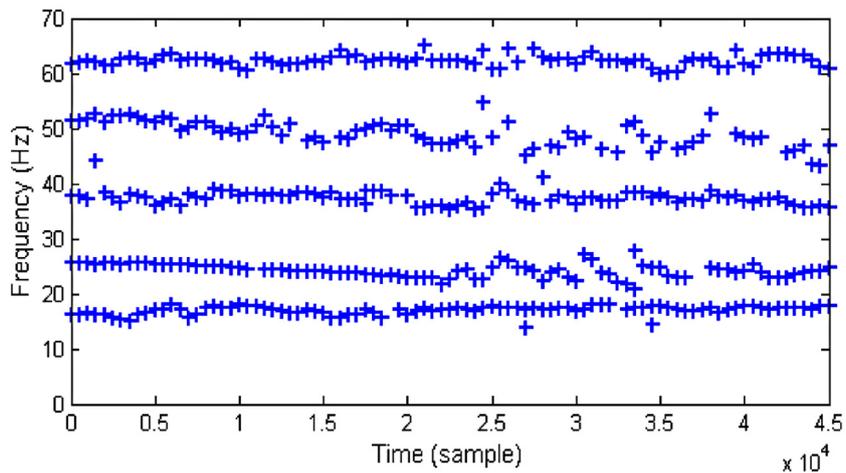


Fig. 9. Frequency monitoring during speed variations.

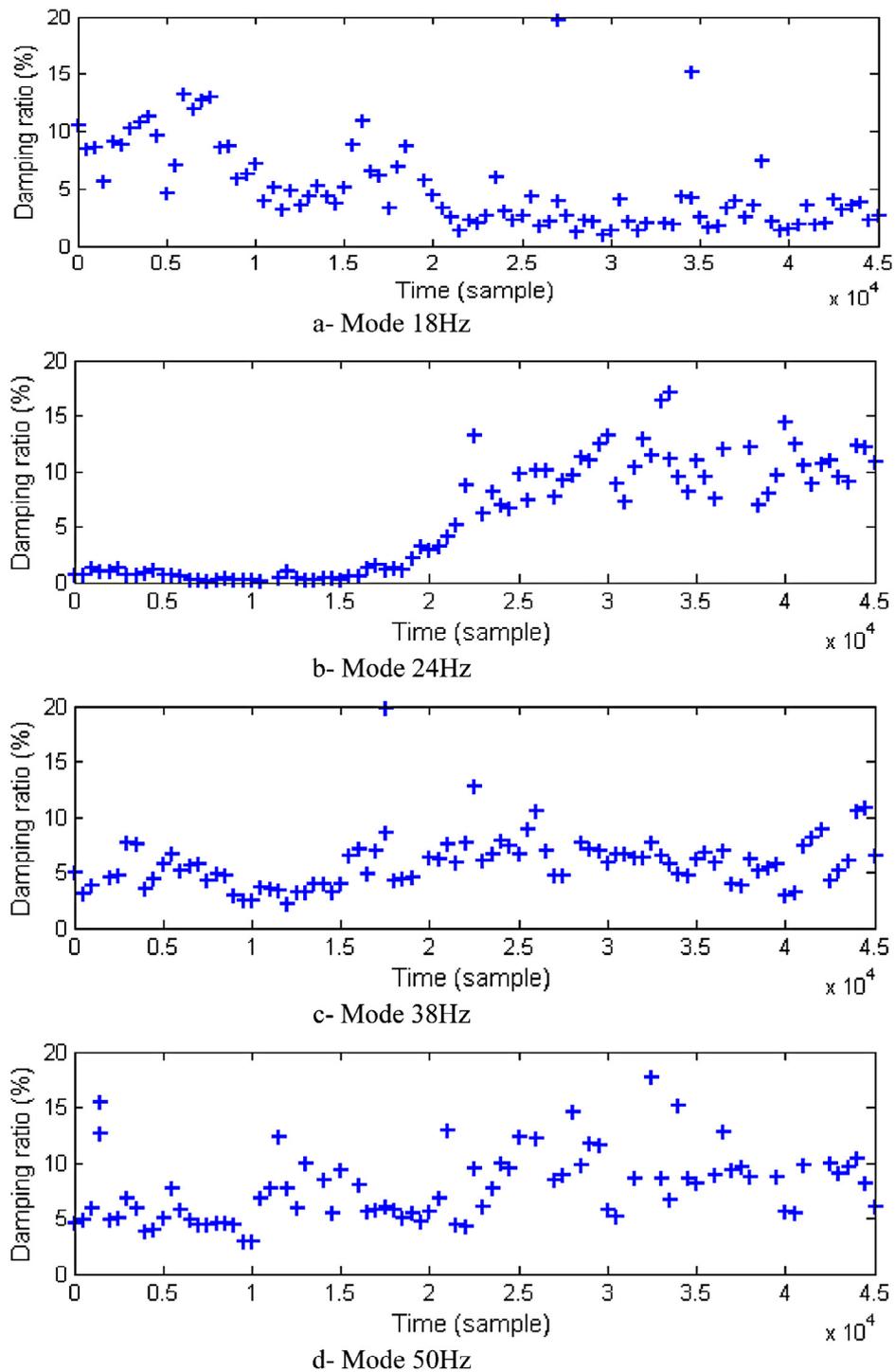


Fig. 10. Damping ratios monitoring during speed variation.

modes. Detail of the modification with the design is ongoing research and is proposed on the part 2 of the project.

### 5.1 Creation of an additional support to the shaft

The shaft is the rotating part of the pump currently has three supports. As the superior part of the pump is

the only accessible location for the modification on the shaft, it is proposed to add a 4th support to the shaft. It is understood that the stiffness of the additional support is limited so several stiffness values are considered. It is found that the linear stiffness of the additional support must be at least  $1E8 \text{ N.m}^{-1}$  to provide a notable change on the natural frequencies. Stiffness at  $1E9 \text{ N.m}^{-1}$  is proposed for the simulation. Figure 11 shows the disposition



Fig. 11. Additional support.

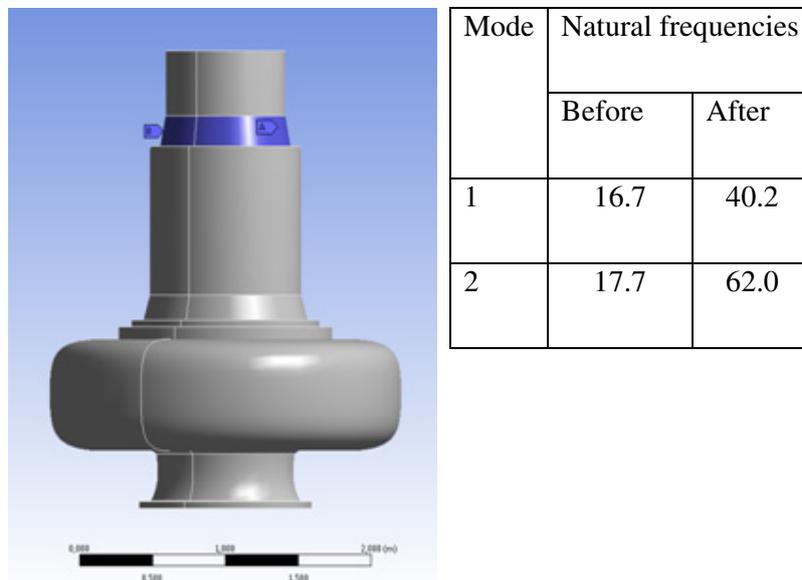


Fig. 12. Chassis reinforcement.

of the current support and the additional support at the top of the shaft. The model presents the numerical natural frequencies before and after installation of the 4th support. It is seen that the natural frequencies are significantly displaced and the resonance at the 3rd and 4th harmonics are avoided.

## 5.2 Chassis reinforcement

Another solution is on the fixed part, the chassis of the pump. It is seen that the lower part of the chassis is fixed to the concrete foundation. However the upper part is more flexible. A structural solution can be considered to

add the steel beam connecting the chassis to the concrete wall in order to reinforce its stiffness. Figure 12 presents the chassis model with the ring support at the upper part. As similar to the shaft, a linear stiffness at  $1E9 \text{ N.m}^{-1}$  is proposed showing the change on the natural frequencies of the chassis itself. It is seen that the resonance on the chassis is avoided effectively.

## 6 Conclusions

Hydraulic pumps are complex industrial structures where the excessive vibrations can be threats to the structural integrity. Operational Modal Analysis (OMA)

adapted for non-stationary systems like STAR can be used for vibration analysis and diagnosis on the heavy industrial machines without knowing of the mechanical and geometric properties, neither the excitation. The method can identify and track accurately the modal parameters during the normal operation of the pump at constant or varying speeds. The rotating speed and the resonance can also be revealed during the monitoring. By combining with the amplitudes assessment, the dynamic picture of the machine is clarified and enlightened to the operators. Several preliminary modifications are also proposed to correct the problem.

## References

- [1] D.J. Ewins, Modal testing: Theory and practice, Research Studies Press, 2000
- [2] N.M.M. Maia, J.M.M. Silva, Modal analysis identification techniques, Royal Society 359-2001 (2001) 9–40
- [3] L. Hermans, H. Van der Auweraer, Modal testing and analysis of structures under operational conditions: Industrial applications, Mech. Syst. Signal Process. 13 (1999) 193–216.
- [4] V.H. Vu, M. Thomas, A.A. Lakis, L. Marcouiller, Short-time autoregressive (STAR) modeling for operational modal analysis of non-stationary mechanical systems, Chapter 3 on book: Vibration and structural acoustic analysis, Springer, 2011, pp. 59–77, ISBN: 978-9400717022
- [5] F. Provost, Rapport d'analyse de vibration, pompe EBARA, Delom Services, 2010, 26 p.
- [6] V.H. Vu, M. Thomas, F. Lafleur, L. Marcouiller, Toward an automatic spectral and modal identification from operational modal analysis, J. Sound Vibr. Elsevier 332 (2013) 213–227
- [7] V.H. Vu, M. Thomas, A.A. Lakis, L. Marcouiller, Operational modal analysis by updating autoregressive model, Mech. Syst. Signal Process. (MSSP) Elsevier 25 (2011) 1028–1044
- [8] V. H. Vu, M. Thomas, F. Lafleur, Harmonic and Modal Frequency Discrimination in Time Domain Operational Modal Analysis, Mechanics & Industry 15 (2014) 29–37
- [9] V.H. Vu, M. Thomas, Uncertainty of modal parameters by operational modal analysis, Mechanics & Industry 15 (2014) 153–158
- [10] B. Badri, V.H. Vu, M. Thomas, Experimental vibration analysis on EBARA pump, Technical Report (in french), ETS, Montreal, 2014, 17 p.
- [11] ISO 10816-7, Mechanical vibration - Evaluation of machine vibration by measurements on non-rotating parts – Part 7: Rotodynamic pumps for industrial applications, including measurements on rotating shafts, 2009, 17 p.
- [12] M. Thomas, Reliability, predictive maintenance and machinery vibration (in french). Presses de l'Université du Québec, 2011, 633 p., D3357, ISBN 978-2-7605-3357-8